

University of Louisville
College of Arts and Sciences

**Department of Physics and Astronomy PhD Qualifying
Examination (Part I)**

Spring 2016

Paper C – Thermal Physics

Time allowed – 90 minutes

Instructions and Information:

- Answer both questions
- This is a closed book examination
- Start each question on a new sheet of paper – use only one side of each sheet
- Write your identification number on the upper right hand corner of each answer sheet
- You may use a non programmable calculator
- Partial credit will be awarded.
- Correct answers without adequate explanations will not receive full credit.
- Make sure your work is legible and clear
- The points assigned to each part of each question is clearly indicated

Thermal Physics Basic

One kg of water at a temperature of 5°C is placed inside an insulated container. [$0^{\circ}\text{C} = 273\text{ K}$]

- (a) How much heat must be extracted to cool the water to 0°C ? (4)
[Specific heat of water = $4200\text{ J/kg}\cdot^{\circ}\text{C}$]
- (b) How much heat must be extracted to freeze all the water? (4)
[Latent heat of fusion of water = $350 \times 10^3\text{ J/kg}$]
- (c) How much heat must be extracted to cool the ice to -28°C ? (4)
[Specific heat of ice = $2000\text{ J/kg}\cdot\text{K}$]

A steel rod is now inserted into the container allowing heat to escape to the surroundings (kept at a constant -28°C) at a rate of 196 Watts.

- (d) How many joules of heat has escaped after 1000 seconds? (4)
- (e) What is the temperature and composition (how much water and how much ice) of the contents of the container after 1000 seconds? (7)
- (f) Evaluate the entropy change of the surroundings after this time. (5)
- (g) Evaluate the entropy change of the water in this time. (7)

Thermal Physics Intermediate

Consider a classical one-dimensional system composed of N localized anharmonic oscillators. The potential energy of each oscillator is given by

$$V(x) = ax^2 + bx^4,$$

where x is the position of the oscillator. Both parameters, a and b , are positive. Assume that b is very small in value and thus can be treated as an expansion parameter. To first order in b , and at a given temperature T ,

- (a) Calculate the partition function of the system. (25)
- (b) Calculate the heat capacity of the system. (20)
- (c) Calculate the average values of x and x^2 . (20)